## Trigonometry

## Curriculum Guide

Scranton School District
Scranton, PA

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## Trigonometry

## Prerequisite: Algebra II, Geometry, Algebra I

Intended Audience: This course is designed for the student who has successfully completed Algebra II by the end of $11^{\text {th }}$ grade.

This course enables students to understand trigonometric principles and to be able to apply then in various fields of mathematics. The topics include a study of functions of angles of any size, radian measure, trigonometric equations, identities, graphing of trigonometric functions, solution of triangles, and the use of various trigonometric formulas.

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Year-at-a-glance
$1^{\text {st }}$ Quarter

| Topic | Resources | CCSS |
| :---: | :---: | :---: |
| 1. Algebra Review <br> Evaluate Algebraic Expressions <br> Determine the Domain <br> Graph Inequalities <br> Laws of Exponents <br> Evaluate Square Roots | - Worksheets <br> - Kuta Software* <br> - Trigonometry: Enhanced with Graphing Utilities Textbook | A1.1.2.1.1 <br> A1.1.3.1.2 <br> A1.1.3.1.1 <br> A2.1.2.1.1 <br> A2.1.2.1.3 |
| 2. Geometry Review <br> Pythagorean Theorem Geometric Formulas | - Worksheets <br> - Kuta Software* <br> - Trigonometry: Enhanced with Graphing Utilities Textbook | G2.1.1.1 <br> G2.1.2.1 <br> G2.2.2.1 <br> G1.2.1.2 <br> G2.2.2.2 <br> G2.2.3.1 |
| 3. Solving Equations With Algebra Solve Linear Equations Factoring Quadratics | - Worksheets <br> - Kuta Software* <br> - Trigonometry: Enhanced with Graphing Utilities Textbook | $\begin{aligned} & \hline A 1.1 .2 .1 .1 \\ & A 2.2 .2 .1 .1 \\ & A 2.2 .2 . .1 .3 \end{aligned}$ |
| 4. Complex Numbers <br> +,-, x,/ Complex Numbers <br> Powers of $i$ | - Worksheets <br> - Kuta Software* <br> - Trigonometry: Enhanced with Graphing Utilities Textbook | A2.1.3.1.1 <br> A2.1.1.1.1 <br> A2.1.1.2.1 <br> A2.1.1.2.2 |

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| 5. Roots, Rational Exponents, Radical Equations <br> Work with Roots <br> Simplify Radicals <br> Rationalize Denominators <br> Solve Radical Equations <br> Simplify Expressions with Rational <br> Exponents | - Worksheets <br> - Kuta Software* <br> - Trigonometry: Enhanced with Graphing Utilities Textbook | $\begin{aligned} & \hline \text { A2.1.3.1.2 } \\ & \text { A2.2.1.1.3 } \end{aligned}$ |
| :---: | :---: | :---: |
| 6. Lines <br> Using Slope, Point Slope, Slope Intercept Graph Lines Write Equations of Lines Parallel and Perpendicular | - Worksheets <br> - Kuta Software* <br> - Trigonometry: Enhanced with Graphing Utilities Textbook | A1.2.2.1.3 |

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| $2^{\text {nd }}$ Quarter |  |  |
| :---: | :---: | :---: |
| Topic | Resources | CCSS |
| 1. Functions and Graphs Use Distance and Midpoint Formulas Graphing Points and Lines by Hand and Graphing Utility | - Worksheets <br> - Kuta Software* <br> - Trigonometry: Enhanced with Graphing Utilities Textbook <br> - Graphing Calculators | $\begin{aligned} & \hline \text { G2.2.1.2.1 } \\ & \text { A1.1.2.1.1 } \\ & \text { A1.1.3.2.2 } \end{aligned}$ |
| 2. Circles <br> Standard Form <br> Graphing Circles by Hand and Graphing Utility | - Worksheets <br> - Kuta Software* <br> - Trigonometry: Enhanced with Graphing Utilities Textbook | $\begin{aligned} & \hline \text { G.1.3.1.1 } \\ & \text { G.1.3.1.2 } \end{aligned}$ |
| 3. Functions <br> Relations - Vertical Line Test <br> Values of Functions Domain of Functions +,-, x,/ of 2 functions | - Worksheets <br> - Kuta Software* <br> - Trigonometry: Enhanced with Graphing Utilities Textbook | A1.1.3.2.2 <br> A2.1.3.1.1 <br> A2.1.3.1.2 <br> A2.1.3.1.3 <br> A2.1.3.1.4 |
| 4. Graphing Techniques Using Vertical and Horizontal Shifts Using Compressions and Stretching | - Worksheets <br> - Kuta Software* <br> - Trigonometry: Enhanced with Graphing Utilities Textbook | A1.2.1.2.1 A1.2.1.2.2 A2.1.3.1.3 A2.1.3.1.4 A2.1.3.2.1 |
| 5. Use of Functions Composite Functions 1 to 1 Functions Inverse Functions | - Worksheets <br> - Kuta Software* <br> - Trigonometry: Enhanced with Graphing Utilities Textbook | A2.2.1.1.2 A2.2.1.1.3 A2.2.1.1.4 A2.2.2.1.1 |

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| Topic | Resources | CCSS |
| :---: | :---: | :---: |
| 1. Angles and their Measure <br> Converting DMS to Decimal, vice versa <br> Arc Length <br> Degrees to Radians, vice versa <br> Area of a sector of a circle <br> Linear Speed | - Worksheets <br> - Kuta Software* <br> - Trigonometry: Enhanced with Graphing Utilities Textbook <br> - Graphing Calculators | $\begin{aligned} & \hline \text { G.2.2.2.2 } \\ & \text { G.2.2.2.3 } \\ & \text { G.2.2.2.5 } \\ & \text { G.2.2.3.1 } \\ & \text { HSF.TF.A. } \end{aligned}$ |
| 2. Right Triangle Trigonometry <br> Values of Acute Angles <br> Complementary Angle Theorem | - Worksheets <br> - Kuta Software* <br> - Trigonometry: Enhanced with Graphing Utilities Textbook <br> - Graphing Calculators | $\begin{aligned} & \text { HSG.SRT.C. } 8 \\ & \text { HSF.TF.C. } 8 \end{aligned}$ |
| 3. Computing Values of Trig Functions <br> Exacts Values of 45,30, 60, <br> Use a Calculator to Approximate | - Worksheets <br> - Kuta Software* <br> - Trigonometry: Enhanced with Graphing Utilities Textbook <br> - Graphing Calculators | HSG.SRT.C. 8 <br> HSF.TF.C. 8 |
| 4. Trig Functions Of General Angles <br> Quadrant Values <br> Terminal Sides <br> Reference Angle <br> Unit Circle | - Worksheets <br> - Kuta Software* <br> - Trigonometry: Enhanced with Graphing Utilities Textbook <br> - Graphing Calculators | HSF.TF.C. 8 <br> HSF.TF.A. 1 <br> HSF.TF.A. 3 |
| 5. Graphs of Trig Functions <br> Sine, Cos, Tan, Csc, Sec, Cot <br> Phase Shifts <br> Curve Fitting | - Worksheets <br> - Kuta Software* <br> - Trigonometry: Enhanced with Graphing Utilities Textbook <br> - Graphing Calculators | HSF.TF.B. 5 HSF.TF.C. 8 |

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| Topic | Resources | CCSS |
| :---: | :---: | :---: |
| 1. Inverses <br> Sine, Cos, Tan | - Worksheets <br> - Kuta Software* <br> - Trigonometry: Enhanced with Graphing Utilities Textbook <br> - Graphing Calculators | HSG.SRT.C. 8 <br> HSF.TF.B. 5 |
| 2. Trigonometric Identities <br> Quotient Identity <br> Reciprocal Identity Pythagorean Identity Sum and Difference Double Angle Half Angle | - Worksheets <br> - Kuta Software* <br> - Trigonometry: Enhanced with Graphing Utilities Textbook <br> - Graphing Calculators | HSF.TF.A. 1 <br> HSF.TF.C. 8 <br> HSF.TF.C. 9 |
| 3. Applications of Right Triangles <br> Law of Sine and Cosines <br> Area of Triangle | - Worksheets <br> - Kuta Software* <br> - Trigonometry: Enhanced with Graphing Utilities Textbook <br> - Graphing Calculators | HSF.TF.B. 5 |
| 4. Polar Coordinates <br> Polar to Rectangular, vice versa Graphing Vectors | - Worksheets <br> - Kuta Software* <br> - Trigonometry: Enhanced with Graphing Utilities Textbook <br> - Graphing Calculators | HSN.CN.B. 4 |

## Curriculum Guide

| General Topic | Academic Standard(s) | Essential Knowledge, Skills \& Vocabulary | Resources \& Activities | Assessments | Suggested Time |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Algebra Review | A1.1.2.1.1 <br> A1.1.3.1.2 <br> A1.1.3.1.1 <br> A2.1.2.1.1 <br> A2.1.2.1.3 | - Write, solve and/or apply a linear equation (including problem situations). <br> - Identify or graph the solution set to a linear inequality on a number line. <br> - Write or solve compound inequalities and/or graph their solution sets on a number line (may include absolute value inequalities). <br> - Use exponential expressions to represent rational numbers. <br> - Simplify/evaluate expressions involving multiplying with exponents, powers of powers and powers of products (limit to rational exponents). | Trigonometry: <br> Enhanced with <br> Graphing Utilities <br> Textbook: A-1 <br> Worksheets <br> Kuta Software* | Teacher prepared tests, quizzes, etc. | 5 Days |


| Geometry Review | $\begin{array}{\|l\|} \hline \text { G2.1.1.1 } \\ \text { G2.1.2.1 } \\ \text { G2.2.2.1 } \\ \text { G1.2.1.2 } \\ \text { G2.2.2.2 } \\ \text { G2.2.3.1 } \end{array}$ | - Verify and apply geometric theorems as they relate to geometric figures. <br> - Apply trigonometric ratios to solve problems involving right triangles. <br> - Estimate area, perimeter, or circumference of an irregular figure <br> - Identify and/or use properties of quadrilaterals. <br> - Find the measurement of a missing length given the area, perimeter, or circumference. <br> - Describe how a change in the linear dimension of a figure affects its perimeter, circumference, and area. | Trigonometry: <br> Enhanced with Graphing Utilities Textbook: A-2 <br> Worksheets <br> Kuta Software Geometry * <br> Trigonometry: Enhanced with Graphing Utilities Textbook | 5 Days |
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| Solving Equations with One Variable, Inequalities | $\begin{aligned} & \hline \text { A1.1.2.1.1 } \\ & \text { A2.2.2.1.1 } \\ & \text { A2.2.2.1.3 } \end{aligned}$ | - Write, solve and/or apply a linear equation. <br> - Create, interpret, and/or use the equation, graph, or table of a polynomial function (including quadratics). <br> - Determine, use, and/or interpret minimum and maximum values over a specified interval of a graph of a polynomial, exponential, or logarithmic function. | Trigonometry: <br> Enhanced with Graphing Utilities Textbook: A-3, A-5 <br> Worksheets <br> Kuta Software* | 10 Days |
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| Complex Numbers | A2.1.3.1.1 <br> A2.1.1.1.1 <br> A2.1.1.2.1 <br> A2.1.1.2.2 | - Write and/or solve quadratic equations (including factoring and using the Quadratic Formula). <br> - Simplify/write square roots in terms of $i$ (e.g., $\sqrt{ }-24=2 i \sqrt{ }$ 6). <br> - Add and subtract complex numbers (e.g., (7-3i) - (2 + i) $=5-4 i$ ). <br> - Multiply and divide complex numbers (e.g., (7$3 i)(2+i)=17+i)$. | Trigonometry: <br> Enhanced with <br> Graphing Utilities <br> Textbook: A-3, A-5 <br> Worksheets <br> Kuta Software* | 10 Days |
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| Nth Roots, Radicals | $\begin{aligned} & \text { A2.1.3.1.2 } \\ & \text { A2.2.1.1.3 } \end{aligned}$ | - Solve equations involving rational and/or radical expressions (e.g., $10 /(x+3)+12 /(x$ $-2)=1$ or $x^{2}+21 x=14$ ). <br> - Determine the domain, range, or inverse of a relation. | Trigonometry: Enhanced with Graphing Utilities Textbook: A-6 <br> Worksheets Practice | 10 Days |

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| Lines | A1.2.2.1.3 | - Write or identify a <br> linear equation <br> when given <br> - the graph of the <br> line <br> two points on <br> the line <br> the slope and a <br> point on the line. <br> Note Linear <br> equation may be in <br> point-slope, <br> standard, and/or <br> slope-intercept <br> form. | Trigonometry: <br> Enhanced with <br> Graphing Utilities <br> Textbook: A-7 | Practice <br> Worksheets <br> Graphing <br> Calculators | Graph Paper |
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| Functions/Graphs | $\begin{aligned} & \hline \text { G2.2.1.2.1 } \\ & \text { A1.1.2.1.1 } \\ & \text { A1.1.3.2.2 } \end{aligned}$ | - Use properties of angles formed by intersecting lines to find the measures of missing angles. <br> - Write, solve, and/or apply a linear equation (including problem situations). <br> - Interpret solutions to problems in the context of the problem situation. Note: Limit systems to two linear inequalities. | Trigonometry: <br> Enhanced with Graphing Utilities Textbook: 1.1,1.2 <br> Graph Paper <br> Graphing Calculators | 5 Days |
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| Circles | $\begin{aligned} & \text { G.1.3.1.1 } \\ & \text { G.1.3.1.2 } \end{aligned}$ | - Identify and/or use properties of congruent and similar polygons or solids. <br> - Identify and/or use proportional relationships in <br> - similar figures. | Trigonometry: <br> Enhanced with <br> Graphing Utilities <br> Textbook: 1.3 <br> Graphing <br> Calculators <br> Graph Paper | 7 Days |

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| Functions | $\begin{array}{\|l} \hline \text { A1.1.3.2.2 } \\ \text { A2.1.3.1.1 } \\ \text { A2.1.3.1.2 } \\ \text { A2.1.3.1.3 } \\ \text { A2.1.3.1.4 } \end{array}$ | - Interpret solutions to problems in the context of the problem situation. Note: Limit systems to two linear inequalities. <br> - Write and/or solve quadratic equations (including factoring and using the Quadratic Formula). <br> - Solve equations involving rational and/or radical expressions (e.g., $10 /(x+3)+12 /(x-$ <br> 2) $=1$ or $x^{2}+21 x=14$ ). <br> - Write and/or solve a simple exponential or logarithmic equation (including common and natural logarithms). <br> - Write, solve, and/or apply linear or exponential growth or decay. | Trigonometry: <br> Enhanced with <br> Graphing Utilities <br> Textbook: 1.4 <br> Graphing <br> Calculators | 7 Days |
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| Graphing Techniques | A1.2.1.2.1 A1.2.1.2.2 A2.1.3.1.3 A2.1.3.1.4 A2.1.3.2.1 | - Create, interpret, and/or use the equation, graph, or table of a linear function. <br> - Translate from one representation of a linear function to another (i.e., graph, table, and equation). <br> - Write and/or solve a simple exponential or logarithmic equation (including common and natural logarithms). <br> - Write, solve, and/or apply linear or exponential growth or decay (including problem situations). <br> - Determine how a change in one variable relates to a change in a second variable (e.g., $y=4 / x$; if $x$ doubles, what happens to $y$ ?). | Trigonometry: Enhanced with Graphing Utilities Textbook: 1.5, 1.6, 1.7 <br> Graphing Calculators <br> Graph Paper | 5 Days |
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| Use of Functions | A2.2.1.1.2 A2.2.1.1.3 A2.2.1.1.4 A2.2.2.1.1 | - Identify and/or extend a pattern as either an arithmetic or geometric sequence (e.g., given a geometric sequence, find the 20th term). <br> - Determine the domain, range, or inverse of a relation. <br> - Identify and/or determine the characteristics of an exponential, quadratic, or polynomial function (e.g., intervals of increase/decrease, intercepts, zeros, and asymptotes). <br> - Create, interpret, and/or use the equation, graph, or table of a polynomial function (including quadratics). | Trigonometry: <br> Enhanced with <br> Graphing Utilities <br> Textbook: 1.8 | 5 Days |
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| Angles and Their Measure | $\begin{aligned} & \hline \text { G.2.2.2.2 } \\ & \text { G.2.2.2.3 } \\ & \text { G.2.2.2.5 } \\ & \text { G.2.2.3.1 } \\ & \text { HSF.TF.A. } \end{aligned}$ | - Find the measurement of a missing length, given the perimeter, circumference, or area. <br> - Find the side lengths of a polygon with a given perimeter to maximize the area of the polygon. <br> - Find the area of a sector of a circle. <br> - Describe how a change in the linear dimension of a figure affects its perimeter, circumference, and area. <br> - Understand radian measure of an angle as the length of the arc on the unit circle subtended by the angle. | Trigonometry: <br> Enhanced with <br> Graphing Utilities <br> Textbook: 2.1 <br> Graphing <br> Calculators | 10 Days |
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| Right Triangle Trigonometry | HSF.TF.A. 3 HSG.SRT.C. 8 HSF.TF.C. 8 | - Use special angles to determine geometrically the values of sine, cosine, tangent for 30,45 , and 60 and use the unit circle to express the values of sine, cosine, and tangent for $\mathbf{x}, \mathbf{x}+\pi$ and $2 \pi-x$ in terms of their values for x , where x is any real number <br> - Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems <br> - Prove the Pythagorean identity $\sin ^{2}(\theta)+$ $\cos ^{2}(\theta)=1$ and use it to find $\sin (\theta)$, $\cos (\theta)$, or $\tan (\theta)$ given $\sin (\theta)$, $\cos (\theta)$, or $\tan (\theta)$ and the quadrant of the angle. | Trigonometry: <br> Enhanced with Graphing Utilities Textbook: 2.2, 2.3 <br> Graphing Calculators | 20 Days |
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| Trigonometric Functions | HSG.SRT.C. 8 <br> HSF.TF.B. 5 <br> HSF.TF.C. 8 <br> HSF.TF.A. 1 | - Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems <br> - Choose <br> trigonometric functions to model periodic phenomena with specified amplitude, frequency, and midline. <br> - Prove the Pythagorean identity $\sin ^{2}(\theta)+$ $\cos ^{2}(\theta)=1$ and use it to find $\sin (\theta)$, $\cos (\theta)$, or $\tan (\theta)$ given $\sin (\theta)$, $\cos (\theta)$, or $\tan (\theta)$ and the quadrant of the angle. <br> - Understand radian measure of an angle as the length of the arc on the unit circle subtended by the angle. | Trigonometry: <br> Enhanced with <br> Graphing Utilities <br> Textbook: 2.4-2.7 <br> Graphing <br> Calculators <br> Unit Circle <br> Computer Graphing Programs | 20 Days |
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| Inverses | HSG.SRT.C.8 <br> HSF.TF.B.5 | Qse trigonometric <br> ratios and the <br> Pythagorean <br> Theorem to solve <br> right triangles in <br> applied problems <br> Choose <br> trigonometric <br> functions to model <br> periodic <br> phenomena with <br> specified <br> amplitude, <br> frequency, and <br> midline. | Trigonometry: <br> Enhanced with <br> Graphing Utilities <br> Textbook: 3.1, 3.2 | Graphing <br> Calculators | 10 Days |
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| Trigonometric Identities | HSF.TF.A. 1 HSF.TF.C. 8 HSF.TF.C. 9 | - Understand radian measure of an angle as the length of the arc on the unit circle subtended by the angle. <br> - Prove the Pythagorean identity $\sin ^{2}(\theta)+$ $\cos ^{2}(\theta)=1$ and use it to find $\sin (\theta)$, $\cos (\theta)$, or $\tan (\theta)$ given $\sin (\theta)$, $\cos (\theta)$, or $\tan (\theta)$ and the quadrant of the angle. <br> - Prove the addition and subtraction formulas for sine, cosine, and tangent and use them solve problems | Trigonometry: <br> Enhanced with <br> Graphing Utilities <br> Textbook: 3.3, 3.4, <br> 3.8 <br> Formulas in <br> Trigonometry: <br> Enhanced with <br> Graphing Utilities <br> Textbook | 10 Days |
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| Applications of Trigonometric Functions with Triangles | HSF.TF.B. 5 | - Choose trigonometric functions to model periodic phenomena with specified amplitude, frequency, and midline. | Trigonometry: <br> Enhanced with <br> Graphing Utilities <br> Textbook: 4.1-4.4 <br> Calculators <br> Formulas Of Laws of Sines, Cosines <br> Areas Formulas (Heron's) | 10 Days |
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| Polar Coordinates | HSN.CN.B. 4 | - Represent complex numbers on the complex plane in rectangular and polar form (including real and imaginary numbers), and explain why the rectangular and polar forms of a given complex number represent the same number. | Trigonometry: <br> Enhanced with <br> Graphing Utilities <br> Textbook: 5.1-5.2 <br> Graphing <br> Calculators <br> Graph Paper | 10 Days |
| Final Exam Preparation |  |  |  | 14 Days |

* Kutasoftware.com - Test and Worksheet Generators for Math Teachers

